

# A Low-Loss 5 GHz Bandpass Filter Using HTS Quarter-Wavelength Coplanar Waveguide Resonators

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**SUMMARY** A new structure of a low-loss high temperature superconducting (HTS) filter is proposed by using quarter-wavelength coplanar waveguide (CPW) resonators. A 4-pole Chebyshev band-pass filter with the center frequency 5.0 GHz and the 0.01 dB-ripple fractional bandwidth 3.2% is designed based on the theory of direct-coupled resonator filters using  $K$ - and  $J$ -inverters. This filter is fabricated by using a high- $T_c$  superconductive YBCO film deposited on a MgO dielectric substrate. The frequency response of the filter measured at 60 K agrees very well with the theoretical one. The insertion loss is 0.22 dB. The insertion loss of this filter is the lowest in HTS-CPW filters presented so far.

**key words:** superconductor, coplanar waveguide, quarter-wavelength resonator, band-pass filter, microwave

## 1. Introduction

The microwave filters using HTS film have the advantages of low-loss, small-size and steep skirt slope characteristics. They are expected to be useful for applications to base stations of mobile communication systems. Many HTS microstrip filters have been developed so far. Compared to these microstrip filter structures, coplanar waveguide (CPW) filter structures are expected to offer the advantages of cost-effective chip processing and easy integration with active devices, because the CPW structure has a HTS film on only one side of the substrate. A High-Q CPW half-wavelength resonator has been reported in [1]. Few papers have been published for HTS filters using CPW half-wavelength resonators [2]–[4]. For these filters, however, low loss characteristics have not been realized, because of radiation loss from the curve sections and excess loss by the conductor airbridges used to suppress the parasitic even mode of CPW.

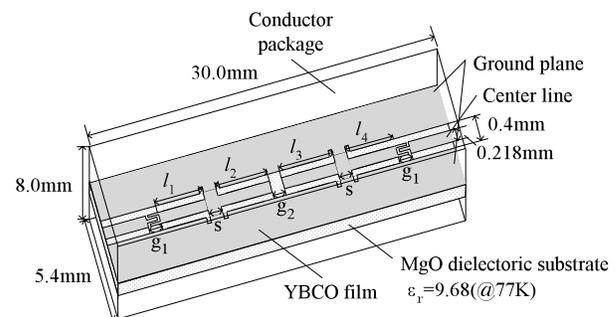
In this paper, a new structure using HTS CPW quarter-wavelength resonators is proposed to realize low insertion loss. In this filter structure, we do not use airbridges which cause the excess conductor loss and curve sections which cause the radiation loss. The quarter-wavelength resonators are available to realize

multi-stage filters because they have half length compared with the half-wavelength resonators. A 4-pole Chebyshev band-pass filter with the center frequency 5.0 GHz and the 0.01 dB-ripple fractional bandwidth 3.2% is designed based on the theory of direct-coupled resonator filters using  $K$ - and  $J$ -inverters. The validity of the design theory will be verified by frequency characteristics measured for the fabricated filter.

## 2. Filter Structure

A structure of a 4-pole BPF using CPW quarter-wavelength resonators is shown in Fig. 1. This filter is constructed by using a high- $T_c$  superconductive YBCO film with the thickness  $0.5 \mu\text{m}$  deposited on a MgO dielectric substrate. The MgO substrate has a dielectric constant  $\epsilon_r = 9.68$  at 77 K and the thickness  $h = 0.5 \text{ mm}$ . This filter is inserted into a Cu conductor package, where the cross sectional dimensions are  $5.4 \text{ mm} \times 8.0 \text{ mm}$  to construct a  $\text{TE}_{10}$  mode cutoff waveguide. The distances between the CPW and the top of the package, and between the substrate and the bottom of the package are 4.5 mm and 3.0 mm, respectively.

The influence of thickness and kinetic inductance of a YBCO film is neglected in this design. The width of the center line is 0.218 mm and the distance between the two ground planes is 0.400 mm, so that the characteristic impedance  $Z_0$  is  $50 \Omega$ . Each of the lengths  $l_1$  to  $l_4$  is approximately one quarter wavelength for the CPW dominant mode. One end of the resonator is terminated by an open gap and the other end is terminated by a short-circuited stub. Couplings between the input port



**Fig. 1** Structure of 4-pole BPF using CPW quarter-wavelength resonators.

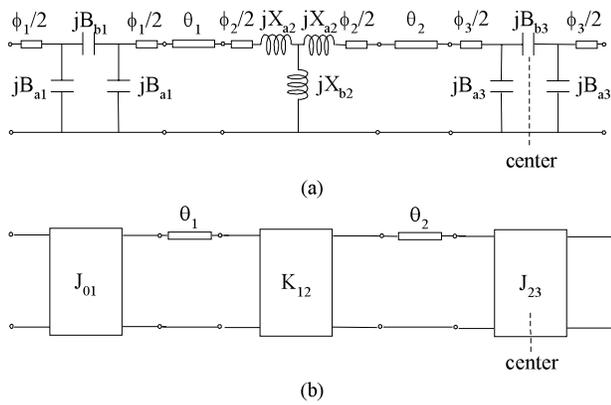
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**Fig. 2** Equivalent circuits of 4-pole quarter-wavelength resonator filter.

and the first resonator and between the second and the third resonator are performed capacitively. Coupling between the first and the second resonator is performed inductively.

The equivalent circuit is shown in Fig. 2(a), which indicates only a half because of the symmetrical structure. Each of the resonators in the equivalent circuit is represented by a uniform transmission line of electrical length  $\theta_i = \pi/2$  ( $i = 1, 2, 3, 4$ ). The open gaps are represented by the equivalent  $\Pi$ -type circuits of the capacitances. Following the design method of direct-coupled resonator filters [5], we can realize  $J$ -inverters by adding the uniform transmission lines of electrical length  $\phi_i$  to both sides of the  $\Pi$ -type circuits. The short-circuited stubs are represented by equivalent  $T$ -type circuits of inductances.  $K$ -inverters are realized in a similar way to the  $J$ -inverters. The equivalent circuit is transformed as shown in Fig. 2(b) by using  $J_{01}$ ,  $J_{23}$ ,  $J_{45}$  inverters and  $K_{12}$ ,  $K_{34}$  inverters.

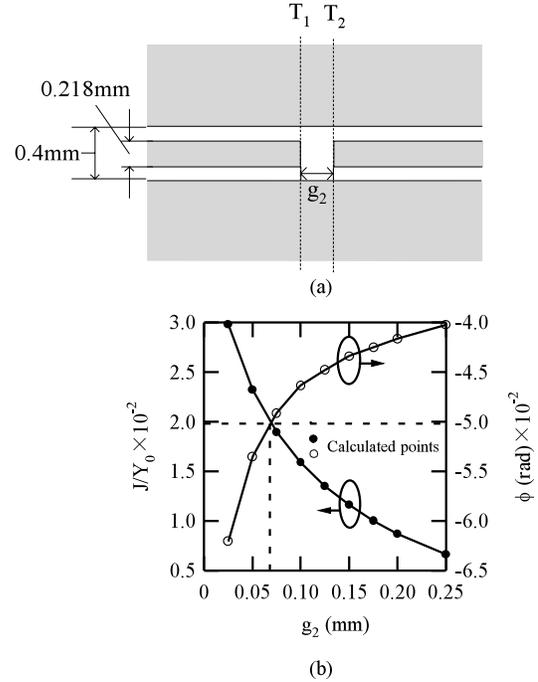
### 3. Design of 4-Pole Filter

When a center frequency  $f_0$ , a ripple width RW, and a fractional ripple pass-band width  $\Delta f/f_0$  are given as this 4-pole filter specification, the design procedure is given as follows:

#### (A) Design of open gap

An open gap structure for  $J_{23}$  is shown in Fig. 3(a). Reference planes  $T_1$  and  $T_2$  shown in the figure correspond to the input and the output port of the equivalent  $\Pi$ -type circuit, respectively. The scattering parameters with different gap width  $g_2$  are computed at  $T_1$  and  $T_2$ , by using 2.5 dimensional electromagnetic simulator SONNET em [7]. From the computed scattering parameters, we obtain element values  $B_a$  and  $B_b$  of the equivalent  $\Pi$ -type circuit from

$$jB_a = \frac{(1 - S_{11})(1 + S_{22}) + S_{12}S_{21} - 2S_{12}}{\Delta} \quad (1)$$



**Fig. 3** (a) Structure of open gap. (b)  $J/Y_0$  and  $\phi$  vs. gap width  $g_2$ .

$$jB_b = \frac{2S_{21}}{\Delta}, \quad (2)$$

where

$$\Delta = (1 + S_{11})(1 + S_{22}) - S_{12}S_{21} \quad (3)$$

From these values, values of  $\phi$  and  $J/Y_0$  in the  $J$ -inverter are calculated from [5]

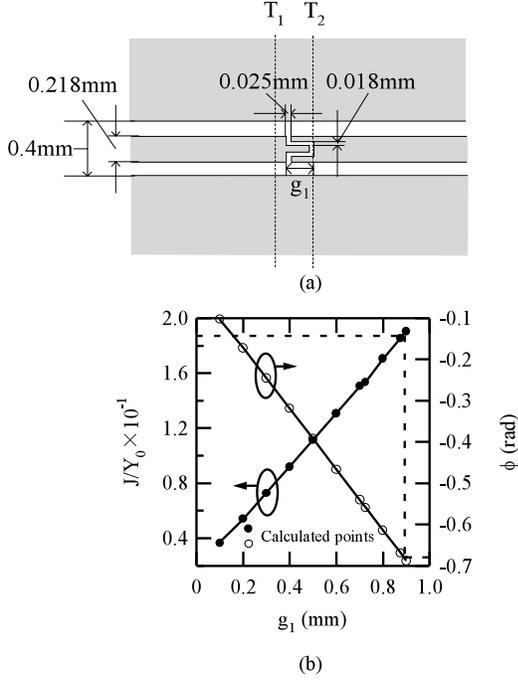
$$\phi = -\tan^{-1} \left( \frac{2B_b}{Y_0} + \frac{B_a}{Y_0} \right) - \tan^{-1} \left( \frac{B_a}{Y_0} \right) \quad (4)$$

$$\frac{J}{Y_0} = \left| \tan \left\{ \frac{\phi}{2} + \tan^{-1} \left( \frac{B_a}{Y_0} \right) \right\} \right| \quad (5)$$

where  $Y_0 = 1/Z_0$ . These values calculated as a function of the gap width  $g_2$  are shown in Fig. 3(b). The solid and open dots in the figure indicate the calculated points.

#### (B) Design of interdigital gaps

We require coupling values for  $J_{01}$  and  $J_{45}$  about 10 times greater, compared with one for  $J_{23}$ , as mentioned below. Then, interdigital gaps with fixed finger spacing 0.025 mm and 0.018 mm were used as shown in Fig. 4(a) to realize the greater coupling values for  $J_{01}$  and  $J_{45}$ . In the interdigital gaps, right and left shunt capacitances of the equivalent  $\Pi$ -type circuit are not equal, because of the asymmetrical structure of left and right hand sides. We first put the reference plane  $T_2$  at the location indicated in Fig. 4(a). Then, to obtain the symmetrical equivalent  $\Pi$ -type circuit, the reference plane



**Fig. 4** (a) Structure of interdigital gap. (b)  $J/Y_0$  and  $\phi$  vs. gap width  $g_1$ .

$T_1$  is determined from

$$T_1 = T_2 - \frac{\angle(S_{11}) - \angle(S_{22})}{8\pi} \lambda_{eff}, \quad (6)$$

where  $\lambda_{eff}$  is an effective wavelength in the CPW at  $f_0$ . Values of  $\phi$  and  $J/Y_0$  are calculated from (1)–(5). These values calculated as a function of the gap width  $g_1$  are shown in Fig. 4(b).

(C) Design of short-circuited stubs

Short-circuited stub for  $K_{12}$  and  $K_{34}$  are shown in Fig. 5(a). The stub has a fixed slot with its width 0.100 mm and depth 0.090 mm to obtain a greater  $K/Z_0$  value. Reference planes  $T_1$  and  $T_2$  shown in the figure correspond to the input and the output port of the equivalent  $T$ -type circuit. The scattering parameters with different stub width  $s$  are computed at  $T_1$  and  $T_2$ . From the computed scattering parameters, we obtain element values  $X_a$  and  $X_b$  of the equivalent  $T$ -type circuit from

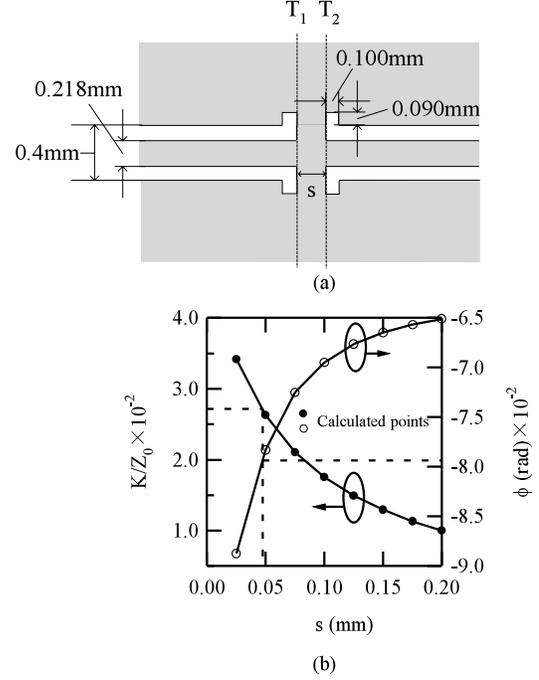
$$jX_a = \frac{(1 + S_{11})(1 - S_{22}) + S_{12}S_{21} - 2S_{12}}{\Delta} \quad (7)$$

$$jX_b = \frac{2S_{21}}{\Delta}, \quad (8)$$

where

$$\Delta = (1 - S_{11})(1 - S_{22}) - S_{12}S_{21} \quad (9)$$

From these values, values of  $\phi$  and  $K/Z_0$  in the  $K$ -inverter are calculated from [5]



**Fig. 5** (a) Structure of short-circuited stub. (b)  $K/Z_0$  and  $\phi$  vs. stub width  $s$ .

$$\phi = -\tan^{-1} \left( \frac{2X_b}{Z_0} + \frac{X_a}{Z_0} \right) - \tan^{-1} \left( \frac{X_a}{Z_0} \right) \quad (10)$$

$$\frac{K}{Z_0} = \left| \tan \left\{ \frac{\phi}{2} + \tan^{-1} \left( \frac{X_a}{Z_0} \right) \right\} \right| \quad (11)$$

These values calculated as a function of the stub width  $s$  are shown in Fig. 5(b).

(D) Determination of resonator length

Actual lengths of the CPW resonators are determined from [5]

$$\theta_i = \frac{\pi}{2} + \frac{1}{2}(\phi_i + \phi_{i+1}), \quad l_i = \frac{\lambda_{eff}}{2\pi} \theta_i \quad (12)$$

where the electrical length  $\phi_i$  is obtained from Figs. 3(b), 4(b) and 5(b), using the  $J/Y_0$  and  $K/Z_0$  values calculated from the filter specifications.

#### 4. Design of 4-Pole Filter Pattern at 5 GHz

A 4-pole Chebyshev bandpass filter is designed with  $f_0 = 5.0$  GHz,  $RW = 0.01$  dB and  $\Delta f/f_0 = 3.2\%$ . Using element values  $g_i$  of the prototype Chebyshev lowpass filter [5], we determined the  $J$ - and  $K$ -inverter values in this filter to be  $J_{01}/Y_0 = J_{45}/Y_0 = 0.187764$ ,  $K_{12}/Z_0 = K_{34}/Z_0 = 0.0271679$  and  $J_{23}/Y_0 = 0.019956$  [5], [6]. Based on the calculated results mentioned above, we obtain  $g_1 = 0.885$  mm,  $g_2 = 0.070$  mm,  $s = 0.045$  mm,  $l_1 = l_4 = 4.985$  mm, and  $l_2 = l_3 = 6.290$  mm. Dimensions of the filter pattern are shown in Fig. 6.

Frequency responses of the designed filter are

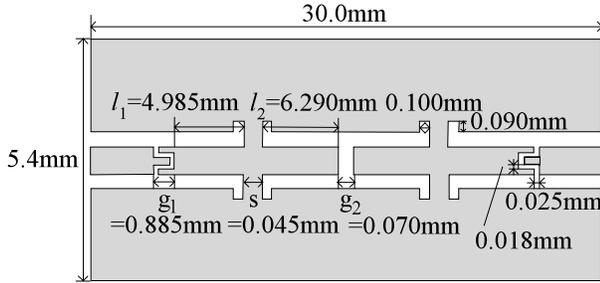
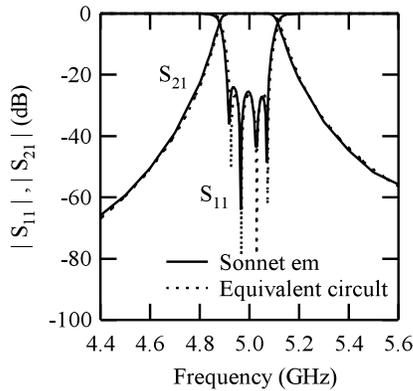
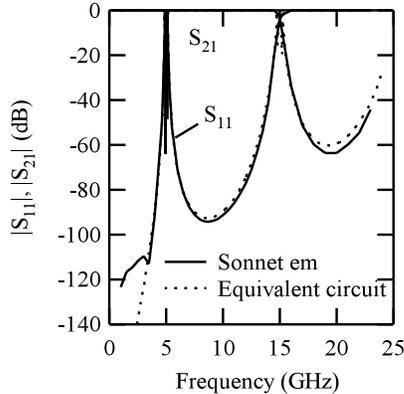


Fig. 6 Dimensions of filter pattern designed.



(a)



(b)

Fig. 7 Simulated frequency responses. (a) Filter response of 4-pole Chebyshev bandpass filter with  $f_0 = 5.0$  GHz,  $RW = 0.01$  dB and  $\Delta f/f_0 = 3.2\%$ . (b) Spurious response.

shown in Fig. 7(a). The solid curve indicates the frequency response simulated from the filter pattern shown in Fig. 6 by using SONNET em [7] and the broken curve indicates one calculated from the equivalent circuit shown in Fig. 2(b). The simulated frequency response agrees very well with one calculated from the equivalent circuit. The spurious frequency responses calculated from SONNET em and the equivalent circuit are shown in Fig. 7(b). The second passband appears about  $3f_0$ , which corresponds to the resonant frequency of the three-fourth-wavelength resonance. No

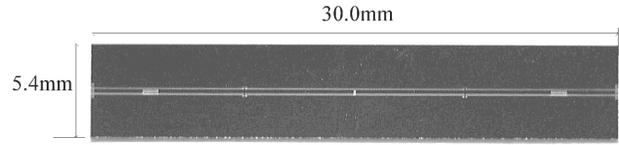


Fig. 8 Photograph of filter pattern fabricated.

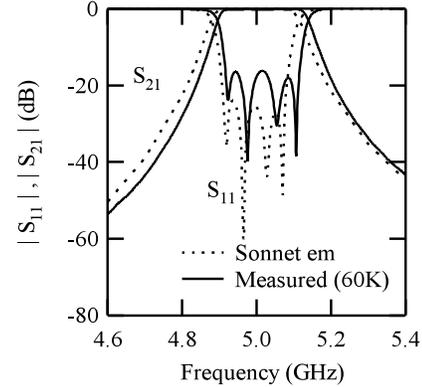


Fig. 9 Measured frequency response.

extra waveguide mode is observed because of the  $TE_{10}$  mode cutoff waveguide constructed by the conductor package.

## 5. Filter Fabrication and Measured Result

Photo lithography and dry etching processes are used to make the filter pattern. A photograph of the filter is shown in Fig. 8. A pair of air coplanar probes is used in the measurement. The frequency response of the filter measured at 60 K is shown in Fig. 9. The measured frequency response agrees very well with the simulated one. The measured results are  $f_0 = 5.02$  GHz and the insertion loss ( $IL$ ) 0.22 dB at 60 K and  $f_0 = 5.00$  GHz and  $IL = 0.32$  dB at 77 K. The equivalent unloaded- $Q$  ( $Q_u$ ) of the resonators calculated from  $IL = 0.22$  dB is 4,300, which is much lower, compared with  $Q_u = 80,000$  reported for 2 GHz microstrip bandpass filter [8]. The following two points are considered as cause of the  $Q$  degradation: 1) Surface resistance ( $R_s$ ) of the superconductor at 5 GHz increases to about 6 times compared with one at 2 GHz because of  $f^2$  characteristic of  $R_s$ . Thus,  $Q_u$  decrease to one-sixth. 2) Excess loss occur at the edges of the grand planes in the CPW structure.

## 6. Conclusion

A new structure of a low-loss HTS filter was proposed by using quarter-wavelength CPW resonators. A 5 GHz Chebyshev band-pass filter was designed based on the theory of direct-coupled resonator filters using  $K$ - and  $J$ -inverters. This filter is fabricated by using a high- $T_c$  superconductive YBCO film deposited on a MgO dielectric substrate. The measured frequency response

agrees very well with the theoretical one, and the validity of the design theory was verified. The insertion loss of this filter was the lowest in HTS-CPW filters presented so far. Finally, the 5 GHz bandpass filter of this structure can be constructed up to a 10-pole filter on a 3-in-diameter YBCO film.

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